FLOW RIPPLE IN EXTERNAL HELICAL GEAR PUMP

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Abstract: This paper presents a flow ripple model for external helical gear pumps. The model is for pumps with and without intermesh side play. Moreover, selected aspects of the evaluation of the acoustic properties of prototype low-noise gear pumps developed in collaboration with the firm PHS HYDROTOR S.A. are described. The acoustic characteristics of the prototype pumps are compared with those of commercially available low-noise pumps.

Key words: external gear pump, low-noise gear pump, flow ripple, noise reduction, helical gear pump

1. Introduction

Displacement pumps, functioning as fluid flow energy generators, are a basic component of hydrostatic drive systems. There are many pump designs, but external gear pumps belong to the most popular ones (Szablowski K., 1997; Osiecki, 2004; Stryczek, 2014).

Most of the current research focuses on system energy efficiency and environmental noise and vibration reduction (Kollek W., 1996; Osinski, 2013; Osiński, 2014). While the efficiency of pumps is quite high for hydraulic equipment, more attention is devoted to the effect of equipment operation on the environment. The main source of noise in pumps, besides the trapped volume and the intermesh, is the flow ripple which generates pressure fluctuations in the whole system. The measure of the flow ripple is pump delivery nonuniformity coefficient δ , which is calculated from the relation:

$$\delta = \frac{Q_{max} - Q_{min}}{Q_t} \tag{1}$$

where: Q_{max} – is the maximum delivery, Q_{min} – the minimum delivery, Q_t – the medium delivery.

2. Flow ripple model

The gear pump belongs to the group of displacement pumps whose principle of operation consists in displacing specified volumes of the fluid from the displacement chambers. In the case of gear pumps, the displacement chambers are the intertooth spaces while the teeth of the counterpart gear are the displacing elements. In order to determine the change in volume dV of the displacement chamber due to tooth entering the intertooth space of the counterpart gear one should carry out a detailed analysis of the geometrical properties of the involute. Analysing this problem on the front face of the intermesh one can determine the change in surface area (dS) caused by the turn of the gears by angle $d\beta$.

As shown in Fig. 1, the initial position at instant t was assumed to be the moment when the teeth's profile is in contact with point e situated at distance $-\overline{Ce}$ from intermesh point C; positive values were conventionally assumed to be situated to the right of this point. The position of the driving wheel is defined by angle β_1 while the position of the driven wheel is defined by angle β_2 .

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Fig. 1: Geometrical properties of intermesh, where: c, d, e, f, g, h – points on the tooth shape, C – pitch point, β_1, β_2 – angular position of gears, $d\beta$ – increment of angle in time dt, α_t – transverse pressure angle, r'_o – effective outside radius, r_t – operating pitch radius, r_b – base radius, l – length of action.

It was assumed that the rotation of the gears by angle $d\beta$ during instant dt would make the intermesh point shift from point e to point f. In the case of helical gears, angular position β_1 of considered cross section dS depends on the position of this cross section relative to the rim's front plane, which can be expressed as $\beta_1 + \gamma(b)$, where γ is the angle of the shift of the cross section situated at distance b relative to the initial cross section. Angle relation $\gamma(b)$ stems from the properties of helical gears and amounts to $\gamma(b) = \frac{\operatorname{tg} \beta_s}{r} b$, where β_s is the angle of inclination of the tooth helix, and r is the pitch radius. The volume of the fluid displaced during time dt will be equal to the integral of the surface area between curves *ceg* and dfh along wheel width db.

$$dV_{\beta} = \int_{0}^{b} \left(dS_{cdef} \left(\beta_{1} + \frac{\operatorname{tg}\beta_{s}}{\operatorname{r}} b \right) + dS_{efgh} \left(\beta_{1} + \frac{\operatorname{tg}\beta_{s}}{\operatorname{r}} b \right) \right) \mathrm{d}b \tag{2}$$

Considering the geometrical properties of the involute and the geometry of the gears one gets:

$$q_{s} = \frac{dV_{\beta}}{dt} = \omega b \left[r'_{o}^{2} - r_{t}^{2} - \frac{1}{12} \left(\frac{r_{b} \operatorname{tg} \beta_{s}}{\operatorname{r}} b \right)^{2} \left(s + \frac{r_{b} \operatorname{tg} \beta_{s}}{2\operatorname{r}} b \right)^{2} \right]$$
(3)

The instantaneous delivery can be related to angle of rotation β , whereby ultimately one gets:

$$q_{s} = \frac{dV_{\beta}}{dt} = \omega b \left[r'_{o}^{2} - r_{t}^{2} - \frac{1}{12} \left(\frac{r_{b} \operatorname{tg} \beta_{s}}{\operatorname{r}} b \right)^{2} \left(r_{b}\beta - \frac{l}{2} + \frac{r_{b} \operatorname{tg} \beta_{s}}{2\operatorname{r}} b \right)^{2} \right]$$
(4)

and for the ideal profile:

$$q_{s} = \frac{dV_{\beta}}{dt} = \omega b \left[r'_{o}^{2} - r_{t}^{2} - \frac{1}{12} \left(\frac{r_{b} \operatorname{tg} \beta_{s}}{\operatorname{r}} b \right)^{2} \left(r_{b}\beta - \frac{t_{b}}{4} - \frac{br_{b} \operatorname{tg} \beta_{s}}{2\operatorname{r}} + \frac{r_{b} \operatorname{tg} \beta_{s}}{2\operatorname{r}} b \right)^{2} \right]$$
(5)

Using the above model of instantaneous delivery and the coefficient of delivery nonuniformity was calculated from relation . Owing to the use of helical gears the flow ripple was reduced from 26.5% to 19.7% for a pump with side play and from 5.9% to 4.2% for a pump without side play (Bury P., Osiński P., 2015).

3. Comparative acoustic tests

Because of difficulties in direct measuring the flow ripple of displacement pumps it was decided to carry out comparative acoustic measurements. Besides prototype units, low-noise pumps and conventional pumps manufactured by leading firms were subjected to the tests. The tested pumps are briefly described in Table 1.

No.	Туре	Description
1	Prototype 2PW-SES	Involute helical gear, no backlash
3	Prototype 2PWR-SE	Involute helical gear, with backlash
4	Commercial conventional	Involute gear, with backlash
5	Commercial low noise 1	Non-involute helical gear, no backlash
6	Commercial low noise 2	Involute helical gear, with backlash
7	Commercial low noise 3	Non-involute helical gear, no backlash

Tab. 1: List of compared pumps and description of their design.

All the hydraulic and acoustic measurements were carried out in the Laboratory of Hydraulic Drives and Machine Vibroacoustics at Wroclaw University of Science and Technology. Measurements of the level of the noise emitted by the gear pumps were carried out in an acoustic diffusion chamber where measurement microphones were set up in eight points. The resultant acoustic pressure level L_m [dB], sound level L_A [dB(A)] and octave spectrum values were read off the microphones and averaged by means of a Brüel&Kjaer apparatus.



Fig. 2: Sound level L_A versus pressure at 1500 rpm.

The sound level adjusted to frequency characteristic A (L_A – Fig. 2) shows that the newly designed pumps have a clear advantage over the conventional pump. Commercial low-noise pumps 1 and 3, with innovative non-involute gears, where the contact between the gears is continuous and no trapped volume forms, emit sound whose level A is considerably lower than that the sound level of the involute gear pumps with backlash (the conventional pump, prototype pump 2PWR-SE and low-noise commercial pump 2). Thanks to the use of skew teeth and zero side play in the 2PW-SES series pumps, combined with the innovative profile optimized by means of logical trees, their sound level A was reduced to the level of the sound emitted by the low-noise non-involute gear pumps under low and medium working pressures p_t . Above 20 MPa the advantage of the non-involute gear pumps is clearer.

4. Conclusion

Due to the limited possibilities of measuring rapidly varied flows, it is difficult to experimentally verify the presented flow ripple model. However, the acoustic tests show a clear reduction in the acoustic pressure level directly connected with sound producing vibrations. The use of helical gears results in maximally a few per cent reduction (depending on the pump design) of the delivery nonuniformity coefficient, but considering the other assets of helical gears, such as their lower intermesh noisiness and gentler change in intermesh stiffness, its effects are satisfactory at no significant increase in production costs, as opposed to the costs of manufacture of non-involute gears.

Moreover, the acoustic parameters, especially sound level L_A , are, as the project assumed, within the low-noise pump range. The comparative tests have shown that the new low-noise 2PW-SES pumps in almost the whole pressure range emit noise whose level is by as much as 6 dB(A) lower than that of the pump of similar design (low-pulsation pump 2). It should be noted that in the low and medium pressure range, the 2PW-SES pump generates noise close to that of the pumps with the profile characterized by zero trapped volume. In addition, this pump can work under higher working pressures than the commercially available low-noise pumps.

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